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NEW JERSEY CENTER FOR TEACHING & LEARNING

AP Physics I

Kinematics in 2D

2017-07-19

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Kinematics in One Dimension

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Review of 1-D Kinematics

• Kinematics is the description of how objects move with respect to a defined reference frame.

• Displacement is the change in position of an object.

• Average speed is the distance traveled divided by the time it took; average velocity is the displacement divided by the time.

• Instantaneous velocity is the limit as the time becomes infinitesimally short.

• Average acceleration is the change in velocity divided by the time.

Review of 1-D Kinematics

• Instantaneous acceleration is the limit as the time interval becomes infinitesimally small.

• There are four equations of motion for constant acceleration, each requires a different set of quantities.

$$v = v_{o} + at$$

$$x = x_{o} + v_{o}t + \frac{1}{2}at^{2}$$

$$v^{2} = v_{o}^{2} + 2a(x - x_{o})$$

$$\overline{v} = \frac{v + v_{o}}{2}$$

1 A snapshot of three racing cars is shown on the diagram. All three cars start the race at the same time, at the same place and move along a straight track. As they approach the finish line, which car has the lowest average speed?



Answer

- D All three cars have the same average speed
- ○E I need help



2 A car and a delivery truck both start from rest and accelerate at the same rate. However, the car accelerates for twice the amount of time as the truck. What is the final speed of the car compared to the truck?

- A Half as much
- \bigcirc B Twice as much
- C Four times as much
- One quarter as much
- ○E I need help



3 A car and a delivery truck both start from rest and accelerate at the same rate. However, the car accelerates for twice the amount of time as the truck. What is the traveled distance of the car compared to the truck?

- A Half as much
- B The same
- ○C Twice as much
- D Four times as much
- \bigcirc E I need help





4 A modern car can develop an acceleration four times greater than an antique car like "Lanchester 1800". If they accelerate over the same distance, what would be the velocity of the modern car compared to the antique car?

- ○A Half as much
- B The same
- ○C Twice as much
- O D Four times as much
- ○E I need help



Graphing Motion at Constant Acceleration

In physics, there is another method in addition to algebraic analysis that can be used, called graphical analysis. The formula $v = v_0 + at$ can be interpreted by the graph. We just need to recall our memory from math classes where we already saw a similar formula, y = mx + b.

From these two formulas we can make some analogies:

v -> y (dependent variable of x) v_0 -> b (intersection with vertical axis), t -> x (independent variable), a -> m (slope of the graph- the ratio between rise and run $\Delta y/\Delta x$)

Motion at Constant Acceleration

Below we can find the geometric explanation to the acceleration a $=\Delta v/\Delta t$.

If slope is equal to: $m = \Delta y / \Delta x$

Then consider a graph with velocity on the y-axis and time on the x-axis. What is the slope for the graph on the right?



Motion at Constant Acceleration

The graph on the right has a slope of $\Delta v/\Delta t$, which is equal to acceleration. Therefore, the slope of a velocity vs. time graph is equal to acceleration.



5 The velocity as a function of time is presented by the graph. What is the acceleration?

- ⊖A 0.2 m/s²
- ○B 0.4 m/s²
- OC 0.5 m/s²
- ○D 1.0 m/s²
- ○E I need help





- 6 The velocity as a function of time is presented by the graph.Find the acceleration.
 - Q -4.0 m/s²
 - -3.5 m/s²
 - -3.0 m/s²
 - -2.5 m/s²
 - I need help



Answer



Motion at Constant Acceleration

The acceleration graph as a function of time can be used to find the velocity of a moving object.

When the acceleration is constant it can be shown on the graph as a straight horizontal line.



Motion at Constant Acceleration

In order to find the change in velocity for a certain limit of time we need to calculate the area under the acceleration versus time graph.



The change in velocity during first 12 seconds is equivalent to the shadowed area (4x12 = 48).

The change in velocity during first 12 seconds is 48 m/s.

7 Which of the following statements is true?

- A The object slows down
- B The object moves with a constant velocity
- C The object stays at rest
- D The object is in free fall
- ○E I need help





- 8 The following graph shows acceleration as a function of time of a moving object. What is the change in velocity during first 10 seconds?
- ○A 0 m/s ○B 15 m/s
- ○C 30 m/s
- \bigcirc E I need help



Answer



Analyzing Position vs Time Graphs

Recall earlier in this unit that slope was used to describe motion.

The slope in a position vs. time graph is $\Delta x/\Delta t$, which is equal to velocity.

Therefore, slope is equal to velocity on a position vs. time graph.





Analyzing Position vs Time Graphs

A positive slope is a positive velocity, a negative slope is a negative velocity, and a slope of zero means zero velocity.





A positive velocity means moving in the positive direction, a negative velocity means moving in the negative direction, and zero velocity means not moving at all.

9 The graph represents the relationship between velocity and time for an object moving in a straight line. What is the traveled distance of the object at 9 s?

- ○A 10 m
- **○**B 24 m
- **○C** 36 m
- ⊃D 48 m
- ○E I need help





10 Which of the following is true?



- A The object increases its velocity
- B The object decreases its velocity
- C The object's velocity stays unchanged
- D The object stays at rest
 - E I need help



11 What is the velocity of the object?

- ○A 2 m/s
- OB 4 m/s
- **○C** 6 m/s
- **○**D 8 m/s
- ○E I need help





Free Fall

All unsupported objects fall towards the earth with the same acceleration.

We call this acceleration the "acceleration due to gravity" and it is denoted by g.

 $g = 9.8 \text{ m/s}^2$

Keep in mind, ALL objects accelerate towards the earth at the same rate.

g is a constant!

Free Fall

What happens at thep?



An object is thrown upward with initial velocity, v_o (Click on question for answer.) What happens when it lands?

Free Fall Answers



Free Fall



Free Fall

For any object thrown straight up into the air, what does the velocity vs time graph look like?



12 A ball is thrown straight up from point A it reachesa maximum height at point B and falls back to point C. Which of the following is true about the direction of the ball's velocity and acceleration between A and B?



Answer



13 A ball is thrown straight up from point A it reachesa maximum height at point B and falls back to point C. Which of the following is true about the direction the ball's velocity and acceleration between B and C?





¹⁴ A package is dropped from an air balloon two times. In the first trial the distance between the balloon and the surface is H and in the second trial4H. Compare the time it takes for the package to reach the surface in the second trial to that in the first trial?



- A The time in the second trial is four times greater.
- \bigcirc B The time in the second trial is two times greater.
- C The time in the second trial is four times less.
- O D The time in the second trial is two times less.
- ○E I need help



- 15 An archer practicing with an arrow bow shoots an arrow straight up two times. The first time the initial speed is v_0 and second time he increases the initial sped to $4v_0$. How would you compare the maximum height in the second trial to that in the first trial?
 - A Two times greater
 - B Four times greater
 - C Eight times greater
 - D Sixteen times greater
 - \bigcirc E I need help



Answer



Vectors and Scalars

Scalar - a quantity that has only a magnitude (number or value)

Vector - a quantity that has both a magnitude and a direction

Which of the following are vectors? Scalars?

Quantity	Vector	Scalar
Time		
Distance		
Displacement		
Speed		

- 16 A runner runs halfway around a circular path of radius 10 m. What is the displacement of the runner?
 - $\bigcirc A \quad 0 m$
 - OB 10 m
 - OC 20 m
 - OD 31.4 m
 - ○E I need help





- 17 A runner runs halfwayaround a circular path ofradius 10 m. What is the total traveled distance of the jogger?
 - OA 0m
 - OB 10 m
 - OC 20 m
 - OD 31.4 m
 - ○E I need help


Adding Vectors in Two Dimensions

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Last year, we learned how to add vectors along a single axis. The example we used was for adding two displacements.



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1. Draw the first vector, beginning at the origin, with its tail at the origin.



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1. Draw the first vector, beginning at the origin, with its tail at the origin.

2. Draw the second vector with its tail at the tip of the first vector.



Last year, we learned how to add vectors along a single axis. The example we used was for adding two displacements.

1. Draw the first vector, beginning at the origin, with its tail at the origin.

2. Draw the second vector with its tail at the tip of the first vector.

3. Draw the Resultant (the answer) from the tail of the first vector to the tip of the last.





The direction of each vector matters. For instance, if the second vector had been 2 units to the EAST (not west), we get a different answer.

In this second case, the vector sum of:

5 units to the East plus

2 units to EAST is

7 units to the East .

Adding Vectors in 2-D

But how about if the vectors are along different axes.

For instance, let's add vectors of the same magnitude, but along different axes.

What is the vector sum of:

5 units East plus

2 units North



1. Draw the first vector, beginning at the origin, with its tail at the origin.





1. Draw the first vector, beginning at the origin, with its tail at the origin.

2. Draw the second vector with its tail at the tip of the first vector.

3. Draw the Resultant (the answer) from the tail of the first vector to the tip of the last.





We know the length of both SIDES of the triangle (a and b), but we need to know the length of the HYPOTENUSE (c).

Magnitude of a Resultant

The magnitude of the resultant is equal to the length of the vector.

We get the magnitude of the resultant from the Pythagorean Theorem:

 $c^2 = a^2 + b^2$

or in this case:

 $R^2 = 5^2 + 2^2$ $R^2 = 25 + 4$ $R^2 = 29$

R = $\sqrt{(29)}$ = 5.4 units



- 18 What is the magnitude of the Resultant of two vectors A and B, if A = 8.0 units north and B = 4.5 units east?
 - ⊖A 9.2 units
 - OB 10.4 units
 - OC 12.5 units
 - \bigcirc D 14.0 units
 - \bigcirc E I need help



- 19 What is the magnitude of the Resultant of two vectors A and B, if A = 24.0 units east and B = 15.0 units south?
 - ○A 24.1 units
 - B 28.3 units
 - C 39.0 units
 - \bigcirc D 44.9 units
 - ○E I need help



In physics, we say the direction of a vector is equal to the angle θ between a chosen axis and the resultant.

In Kinematics, we will primarily use the x-axis to measure θ .

However, if we were to change the axis we used and apply the proper mathematical techniques, we should get the same result!



To find the value of the angle θ , we need to use what we already know:

the length of the two sides opposite and adjacent to the angle.

(remember SOH CAH TOA)









20 What is the direction of the Resultant of the two vectors A and B if: A = 8.0 units north and B = 4.5 units east if East is 0° and North is 90°?

⊖A 34.8°

OB 41.4°

OC 53.6°

OD 60.6°

\bigcirc E I need help



- 21 What is the direction (from East) of the Resultant of the two vectors A and B if: A = 24.0 units east and B = 15.0 units south?
 - \bigcirc A 13° South of East
 - \bigcirc B 32° South of East
 - C 40° South of East
 - D 49° South of East
 - \bigcirc E I need help



- 22 Find the magnitude and direction of the resultant of two vectors A and B if:
 - A = 400 units north B = 250 units east
 - Magnitude = ?
 - \bigcirc A 150 units
 - OB 396 units
 - ^OC 472 units
 - \bigcirc D 650 units
 - \bigcirc E I need help



- 23 Find the magnitude and direction of the resultant of two vectors A and B if:
 - A = 400 units north B = 250 units east
 - Direction = ?
 - Q 27° East of North
 - B 32° East of North
 - C 41° East of North
 - 58° East of North
 - \bigcirc E I need help



- 24 A student walks a distance of 300 m East, then walks 400 m North. What is the magnitude of the net displacement?
 - ○A 300 m
 - ○B 400 m
 - OC 500 m
 - $^{igodoldsymbol{O}}$ D 700 m
 - \bigcirc E I need help





- 25 A student walks a distance of 300 m East, then walks 400 m North. What is the total traveled distance?
 - ○A 300 m
 - ○B 400 m
 - OC 500 m
 - ○D 700 m
 - ○E I need help





- 26 Two displacement vectors have magnitudes of 5.0 m and 7.0 m, respectively. When these two vectors are added, the magnitude of the sum:
 - ○A is 2.0 m.
 - \bigcirc B could be as small as 2.0 m, or as large as 12 m.
 - OC is 12 m.
 - \bigcirc D is larger than 12 m.
 - \bigcirc E I need help



- 27 The resultant of two vectors is the largest when the angle between them is
 - ○A 0°
 - OB 45°
 - OC 90°
 - OD 180°
 - ○E I need help



- 28 The resultant of two vectors is the smallest when the angle between them is:
 - ○A 0°
 - OB 45°
 - OC 90°
 - OD 180°
 - ○E I need help

Basic Vector Operations

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Adding Vectors in the opposite order gives the same resultant.

 $V_1 + V_2 = V_2 + V_1$



Even if the vectors are not at right angles, they can be added graphically by using the "tail to tip" method.

The resultant is drawn from the tail of the first vector to the tip of the last vector.





Subtracting Vectors

In order to subtract a vector, we add the negative of that vector. The negative of a vector is defined as that vector in the opposite direction.



Multiplication of Vectors by Scalars

A vector V can be multiplied by a scalar c. The result is a vector cV which has the same direction as V. However, if c is negative, it changes the direction of the vector.



- 29 Which of the following operations will not changea vector?
 - OA Translate it parallel to itself
 - OB Rotate it
 - ○C Multiply it by a constant factor
 - O D Add a constant vector to it
 - ○E I need help



Vector Components

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Any vector can be described as the sum as two other vectors called components. These components are chosen perpendicular to each other and can be found using trigonometric functions.



In order to remember the right triangle properties and to better identify the functions, it is often convenient to show these components in different arrangements (notice v = y below).



- 30 If a ball is thrown with a velocity of 25 m/s at an angle of 37° above the horizontal, what is the vertical component of the velocity?
 - ○A 12 m/s
 - ○B 15 m/s
 - OC 20 m/s
 - ○D 25 m/s
 - E I need help





- 31 If a ball is thrown with avelocity of 25 m/s at anangle of 37° above the horizontal, what is the horizontal component of thevelocity?
 - ○A 12 m/s
 - ○B 15 m/s
 - OC 20 m/s
 - ○D 25 m/s
 - ○E I need help





32 If you walk 6.0 km in a straight line in a direction north of east and you end up 2.0 km north and several kilometers east. How many degrees north of east have you walked?

Answer

- OA 19°
- OB 45°
- OC 60°
- OD 71°
- ○E I need help



Using the tip-to-tail method, we can sketch the resultant of any two vectors.



But we cannot find the magnitude of 'v', the resultant, since v_1 and v_2 are two-dimensional vectors

We now know how to break v_1 and v_2 into components...



And since the x and y components are one dimensional, they can be added as such.





1. Draw a diagram and add the vectors graphically.



- 1. Draw a diagram and add the vectors graphically.
- 2. Choose x and y axes.



У

- 1. Draw a diagram and add the vectors graphically.
- 2. Choose x and y axes.
- 3. Resolve each vector into x and y components.



У

- 1. Draw a diagram and add the vectors graphically.
- 2. Choose x and y axes.
- 3. Resolve each vector into x and y components.
- 4. Calculate each component.

 $v_{1x} = v_1 \cos(\theta_1) v_{2x} = v_2 \cos(\theta_2)$

 $v_{1y} = v_1 \sin(\theta_1) v_{2y} = v_2 \sin(\theta_2)$



- 1. Draw a diagram and add the vectors graphically.
- 2. Choose x and y axes.
- 3. Resolve each vector into x and y components.
- 4. Calculate each component.
- 5. Add the components in each direction.



- 1. Draw a diagram and add the vectors graphically.
- 2. Choose x and y axes.
- 3. Resolve each vector into x and y components.
- 4. Calculate each component.
- 5. Add the components in each direction.
- 6. Find the length and direction of the resultant vector.

- 1. 24m, 30° north of east
- 2. 28m, 37° east of north
- 3. 20m, 50° west of south





$$d_{1v} = 24m\sin 30^\circ = 12m$$



$$d_{2y} = 28m\cos 37^\circ = 22.4m$$



Now we can put the components in a chart and solve for the resultant vector.

	x (m)	y (m)
d ₁	20.8	12.0
d ₂	16.9	22.4
d ₃	-15.3	-12.9
Σ	22.4	21.5

To find the magnitude of the resultant, use the Pythagorean theorem.

$$c^{2} = a^{2} + b^{2}$$

 $c = \sqrt{(22.4m)^{2} + (21.5m)^{2}} = 31m$

To find the direction of the resultant, use inverse tangent.

$$\tan \theta = \frac{opposite}{adjacent}$$
$$\theta = \tan^{-1} \frac{21.5}{22.4} = 43.8^{\circ}$$

- 33 Graphically determine the magnitude and direction of the resultant of the following three vector displacements:
 - 1. 15 m, 30° north of east
 - 2. 20 m, 37° north of east
 - 3. 25 m, 45 north of east
 - Magnitude = ?
 - Q 60.0 m
 - ○B 72.4 m
 - 85.3 m
 - 92.0 m



○ I need help

- 34 Graphically determine the magnitude and direction of the resultant of the following three vector displacements:
 - 1. 15 m, 30° north of east
 - 2. 20 m, 37° north of east
 - 3. 25 m, 45 north of east

Direction = ?

- Q 29.4°
- 38.6°
- OC 42.9°
 - 50.3°



○E I need help

- 35 Which of the following is an accurate statement?
 - ○A A vector cannot have a magnitude of zero if one of its components is not zero.
 - B The magnitude of a vector can be equal to less than the magnitude of one of its components.
 - If the magnitude of vector A is less than the magnitude of vector B, then the x-component
 - of A must be less than the x-component of B.
 - **OD** The magnitude of a vector can be either positive or negative.



I need help



Demo

Projectile Motion

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Projectile Motion: 1st Type

A projectile is an object moving in two dimensions under the influence of Earth's gravity. Its path is a parabola.



Projectile Motion: 1st Type

Projectile motion can be understood by analyzing the vertical and horizontal motion separately.

The speed in the x-direction is constant.

The speed in the y-direction is changing.



A mountain lion leaps horizontally from a 7.5 m high rock with a speed of 4.5 m/s. How far from the base of the rock will he land?

A mountain lion leaps horizontally from a 7.5 m high rock with a speed of 4.5 m/s. How far from the base of the rock will he land?

First, determine the time it will take for the lion to reach the ground.

 $v_{0y} = 0 \qquad y = y_0 + v_{0y}t + \frac{1}{2}a_yt^2$ $a_y = -9.8\frac{m}{s^2} \qquad 0 = y_0 + \frac{1}{2}a_yt^2$ $y_0 = 7.5m \qquad t = \sqrt{\frac{-2y_0}{a_y}} = \sqrt{\frac{-2(7.5m)}{(-9.8\frac{m}{s^2})}} = 1.24s$ A mountain lion leaps horizontally from a 7.5 m high rock with a speed of 4.5 m/s. How far from the base of the rock will he land?

Then, determine how far from the base he will land.

 $v_{0x} = 4.5 \frac{m}{s} \qquad x = x_0 + v_{0x}t + \frac{1}{2}a_xt^2$ $a_x = 0 \qquad x = v_{0x}t = \left(4.5 \frac{m}{s}\right)(1.24s) = 5.6m$ x = ?t = 1.24s

- 36 A cannon ball is shot from a cannon at a height of 15 m with a velocity of 20 m/s. How far away will the cannon ball land?
 - 🔾 35 m
 - 50 m
 - 60 m
 - 65 m
 - I need help

37 A marble rolls off a table from a height of 0.8 m with a velocity of 3 m/s. Then another marble rolls off the same table with a velocity of 4 m/s. Which values are the same for both marbles?

Justify your answer qualitatively, with no equations or calculations.

- \bigcirc A The final speeds of the marbles.
- \bigcirc B The time each takes to reach the ground.
- C The distance from the base of the table where each lands.
- ○D I need help

Projectile Motion: 2nd Type

If an object is launched at an angle with the horizontal, the analysis is similar except that the initial velocity has a vertical component.





Projectile motion can be described by two kinematics equations:

horizontal component:

vertical component:

$$x = x_0 + v_{0x}t + \frac{1}{2}a_xt^2 = v_0\cos\theta t$$
$$v_x = v_{0x}t + a_xt = v_0\cos\theta$$
$$a_x = 0$$

$$y = y_0 + v_{0y}t + \frac{1}{2}a_yt^2 = v_o\sin\theta t - \frac{1}{2}gt^2$$
$$v_y = v_{0y}t + a_yt = v_0\sin\theta - gt$$
$$a_y = g$$

Flying time:

$$y = v_{o} \sin \theta t - \frac{1}{2}gt^{2}$$

$$x = v_{0} \cos \theta t$$

$$y = v_{o} \sin \theta t - \frac{1}{2}gt^{2}$$

$$x = v_{0} \cos \theta \frac{2v_{0} \sin \theta}{g}$$

$$t = \frac{t_{total}}{2}$$

$$y = v_{o} \sin \theta t - \frac{1}{2}gt^{2}$$

$$y = v_{o} \sin \theta t - \frac{1}{2}gt^{2}$$

$$y = v_{o} \sin \theta t - \frac{1}{2}gt^{2}$$

$$y = v_{o} \sin \theta \frac{v_{0} \sin \theta}{g} - \frac{1}{2}g\left(\frac{v_{0} \sin \theta}{g}\right)^{2}$$

$$y = \frac{v_{0}^{2} \sin^{2} \theta}{g}$$

$$y = \frac{v_{0}^{2} \sin^{2} \theta}{g}$$

$$y = \frac{v_{0}^{2} \sin^{2} \theta}{2g}$$

- 38 Ignoring air resistance, thehorizontal component of a projectile's velocity:
 - $\bigcirc \mathsf{A}$ is zero.
 - OB remains constant.
 - \bigcirc C continuously increases.
 - OD continuously decreases.
 - CE I need help





- 39 A ball is thrown with a velocity of 20 m/s at an angle of 60° above the horizontal. What is the horizontal component of its instantaneous velocity at the exact top of its trajectory?
 - ○A 10 m/s
 - OB 17 m/s
 - \bigcirc C 20 m/s
 - $\bigcirc \mathsf{D}$ zero
 - \bigcirc E I need help




- 40 Ignoring air resistance, the magnitude of thehorizontal component of a projectile's acceleration:
 - $\bigcirc A$ is zero.
 - \bigcirc B remains a non-zero constant.
 - \bigcirc C continuously increases.
 - OD continuously decreases.
 - ⊖E I need help



- 41 At what angle should a water-gun be aimed in order for the water to land with the greatest horizontal range?
 - ○A 0°
 - OB 30°
 - OC 45°
 - OD 60°
 - ○E I need help

Answer



- 42 (Mulitple Answer) An Olympic athlete throws a javelin at six different angles above the horizontal, each with the same speed: 20°, 30°, 40°, 60°, 70° and 80°. Which two throws cause the javelin to land the same distance away? Be prepared to justify your answer.
 - □A 30° and 80°
 - □B 20° and 70°
 - □C 30° and 70°
 - □D 30° and 60°
 - □ I need help

- 43 You are throwing a ball for the second time. If the ball leaves your hand with twice the velocity it had on your first throw, its horizontal range R (compared to your first serve) would be
 - QA 1.4 R
 - **OB** R/2
 - $\bigcirc C 2R$
 - $\bigcirc D$ 4R
 - ○E I need help





44 When a football in a field goal attempt reaches its maximum height, how does its speed compare to its initial speed? (Justify your answer.)

Answer

- $\bigcirc A$ It is zero.
- \bigcirc B It is less than its initial speed.
- \bigcirc C It is equal to its initial speed.
- \bigcirc D It is greater than its initial speed.
- ○E I need help



- 45 A stone is thrown horizontally from the top of a tower at the same instant a ball is dropped vertically.Which object is traveling faster when it hits the level ground below? (Justify your answer.)
 - ○A It is impossible to tell from the information given.
 - \bigcirc B the stone
 - \bigcirc C the ball
 - \bigcirc D Neither, since both are traveling at the same speed.
 - ○E I need help





46 A plane flying horizontally at a speed of 50.0 m/s and at an elevation of 160 m drops a package. Two seconds later it drops a second package. How far apart will the two packages land on the ground?

Answer

- ○A 100 m
- ○B 170 m
- **○**C 180 m
- ○D 210 m
- ○E I need help



47 An arrow is fired at an angle of θ above the horizontal with a speed of v. Explain how you can calculate the horizontal range and maximum height. (List the steps you would take and the equations you would use so that another student could solve this problem but do not solve the problem.)

Determine the total time in the air.

2 s
3 s
5 s
7 s

○ I need help

Determine the maximum height reached by the projectile.

Q 8.1 m

○ 9.6 m

○ 11 m

○ 13 m

○ I need help

Determine the maximum horizontal distance covered by the projectile.

Q 45 m

○ 61 m

○ 70 m

○ 78 m

○ I need help

Determine the velocity of the projectile 2.0 s after firing.

OA 5.4°

OB 11⁰

^OC 14⁰

OD 19⁰

○E I need help

Projectile Motion: 3rd Type

If an object is launched at an angle with the horizontal and from an initial height, the analysis is similar except when finding the total time in the air. You will need to use the quadratic formula.

$$0 = y_0 + v_o \sin \theta t - \frac{g}{2}t^2$$
$$0 = c + bx + ax^2$$
$$t_{total} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$



Determine the total time in the air.

○A 3.9 s

○B 5.5 s

○C 8.9 s

○D 11 s

○E I need help

Determine the maximum horizontal range.

- Q 120 m
- 190 m
- 200 m
- 250 m
- I need help

Determine the magnitude of the velocity just before impact.

- Q 45 m/s
- ◯ 70 m/s
- 77 m/s
- 90 m/s
- I need help

Determine the angle the velocity makes with the horizontal just before impact.

- ^OA -30⁰
- OB -44∘
- ^OC -72⁰

OD -80°

 \bigcirc E I need help