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NEW JERSEY CENTER FOR TEACHING & LEARNING

Algebra Based Physics

Kinematics in One Dimension

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Motion in One Dimension



https://www.njctl.org/video/?v=ARE0bLtRFVI

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We all know what the distance between two objects is...

So what is it? What is distance? What is length?

ALSO - you can't use the words "distance" or "length" in your definition; that would be cheating.

As you can see from your efforts, it is impossible to define distance.

Distance is a fundamental part of nature. It is so fundamental that it's impossible to define. Everyone knows what distance is, but no one can really say what it is.

However, distances can be compared.



We can compare the distance between two objects to the distance between two other objects.

For convenience, we create standard distances so that we can easily make comparisons... and tell someone else about them.

We will be using the meter as our unit for measuring distance. It's just that it's been accepted as a universal standard, so everyone knows what it is.

This doesn't define distance, but it allows us to work with it.

We'll be using meter as our standard for measuring distance.

The symbol for distance is "d".

And the unit for the meter is "m"



Similarly, everyone knows what time is...

But try defining it; what is time?

Remember you can't use the word "time" or an equivalent to the word "time", in your definition.

Like distance, time is a fundamental aspect of nature.

It is so fundamental that it's impossible to define. Everyone knows what time is, but no one can really say what it is...

However, like distances, times can be compared.

We can say that in the time it took to run around the track, the second hand of my watch went around once...so my run took 60 seconds. When we compare the time between two events to the time between two other events, we are measuring time.



This doesn't define time, but it allows us to work with it.

We will be using the econdas our standard for measuring time.

The symbol for time is "t"

The unit for a second is "s".



Click here a "minute physics" video on measuring time and distance

Speed

Speed is defined as the distance traveled divided by the time it took to travel that distance.

speed = distance
time
$$s = \frac{d}{t}$$

Speed is not a fundamental aspect of nature, it is the ratio of two things that are.

Speed

The units of speed can be seen by substituting the units for distance and time into the equation

$$s = \frac{d}{t}$$

<u>meters</u> seconds

 $\frac{m}{s}$

We read this unit as "meters per second"

- 1 A car travels at a constant speed of 10m/s. This means the car:
 - increases its speed by 10m every second. Α
 - decreases its speed by 10m every second. В
 - moves with an acceleration of 10 meters every second.

 - I need help $\bigcirc \mathsf{E}$



https://www.njctl.org/video/?v=7E8c3jVbN2w

- 2 A rabbit runs a distance of 60 meters in 20 s; what is the speed of the rabbit?
 - Q 0.3 m/s
 - 0.6 m/s
 - 3 m/s
 - 4 m/s

○ I need help





Answer

- 3 An airplane on a runway can cover 500 m in 10 s; what is the airplane's average speed?
 - ⊖A 0.02 m/s
 - ○B 50 m/s
 - OC 100 m/s
 - ○D 5000 m/s
 - \bigcirc E I need help





- 4 A car travels at a speed of 40 m/s for 4.0 s; what is the distance traveled by the car?
 - Q 4 m
 - 10 m
 - 160 m
 - 320 m

○ I need help





- 5 You travel at a speed of 20m/s for 6.0s; what distance have you moved?
 - Q 6 m
 - 20 m
 - 120 m
 - 160 m
 - I need help





6 You travel at a constant speed of 20 m/s; how much time does it take you to travel a distance of 120m?

^OA 6s

○B 12 s

○C 20 s

○D 60 s

\bigcirc E I need help





- 7 You travel at a constant speed of 30m/s; how much time does it take you to travel a distance of 150m?
 - Q 0.2 s
 - 5 s
 - 15 s
 - ◯ 30 s

○ I need help







Average Speed





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Average Speed

The speed we have been calculating is a constant speed over a short period of time. Another name for this is instantaneous speed.

If a trip has multiple parts, each part must be treated separately. In this case, we can calculate the average speed for a total trip.

Determine the average speed by finding the *total* distance you traveled and dividing that by the *total* time it took you to travel that distance.

Distance and Time Intervals

In physics we use subscripts in order to avoid any confusion with different distances and time intervals.

For example: if an object makes a multiple trip that has three parts we present them as d_1 , d_2 , d_3 and the corresponding time intervals t_1 , t_2 , t_3 .

Average Speed & Non-Uniform Motion

The following pattern of steps will help us to find the average speed:

Find the total distance $d_{total} = d_1 + d_2 + d_3$

Find the total time $t_{stal} = t_1 + t_2 + t_3$

Use the average speed formula $s_{avg} = \frac{d_{total}}{t_{total}}$

Average Speed - Example 1



You ride your bike home from school by way of your friend's house. It takes you 7 minutes (420 s) to travel the 2500 m to his house. You spend 10 minutes there, before traveling 3500 m to your house in 9 minutes (540 s). What was your average speed for this trip?

> To keep things clear, we can use a table (graphic organizer) to keep track of the information...

Write the given information in the table below:

Segment	Distance	Time	Speed
	(m)	(s)	(m/s)
I			
II			
III			
Total /Avg.			

Write the given information in the table below:

Segment	Distance	Time	Speed
	(m)	(s)	(m/s)
I			
II			
Ш			
Total /Avg.			

Write the given information in the table below:

Segment	Distance	Time	Speed
	(m)	(s)	(m/s)
I	2500	420	
II			
111			
Total /Avg.			

Next, use the given information to find the *total* distance and *total* time

Segment	Distance	Time	Speed
	(m)	(s)	(m/s)
I	2500	420	
II	0	600	
III	3500	540	
Total /Avg.			

You ride your bike home from school by way of your friend's house. It takes you 7 minutes (420 s) to travel the 2500 m to his house. You spend 10 minutes (600 s) there, before traveling 3500 m to your house in 9 minutes (540 s). What was your average speed for this trip?

 $\mathbf{d}_{\text{total}} = \mathbf{d}_1 + \mathbf{d}_2 + \mathbf{d}_3$

Next, use the given information to find the *total* distance and *total* time

Segment	Distance	Time	Speed
	(m)	(s)	(m/s)
I	2500	420	
II	0	600	
111	3500	540	
Total /Avg.	6000		

You ride your bike home from school by way of your friend's house. It takes you 7 minutes (420 s) to travel the 2500 m to his house. You spend 10 minutes (600 s) there, before traveling 3500 m to your house in 9 minutes (540 s). What was your average speed for this trip?

 $\mathbf{t}_{\text{total}} = \mathbf{t}_1 + \mathbf{t}_2 + \mathbf{t}_3$

Next use total distance and time to find average speed.

Segment	Distance	Time	Speed
	(m)	(s)	(m/s)
I	2500	420	
II	0	600	
III	3500	540	
Total /Avg.	6000	1560	

$$S_{avg} = d_{total}$$

$$\frac{t_{total}}{t_{total}}$$

Example 1 - Solution

Next use total distance and time to find average speed.

Segment	Distance	Time	Speed
	(m)	(s)	(m/s)
I	2500	420	
II	0	600	
III	3500	540	
Total /Avg.	6000	1560	3.85

$$S_{avg} = \frac{d_{total}}{t_{total}} = \frac{6000 \text{ m}}{1560 \text{ s}} =$$

Example 2

Fill in the Table and Determine Average Speed

Segment	Distance	Time	Speed
	(m)	(s)	(m/s)
I			
II			
111			
Total /Avg.			

You run a distance of 210 m at a speed of 7 m/s. You then jog a distance of 800 m in a time of 235 s. Finally, you run for 25 s at a speed of 6 m/s. What was the average speed of your total run?

Example 2 - Reflection

Segment	Distance	Time	Speed
	(m)	(s)	(m/s)
I	210	30	7
II	800	235	3
II	150	25	6
Total /Avg.	1160	290	4

What happens when you take the 'average' (arithmetic mean) of the speed for each leg of the trip? Is it the same as the average speed?

Why do you think this happens?

Position and Reference Frames



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www.nictl.org/video/?v=5mPK2E2GkzA

Position and Reference Frames

Speed, distance and time didn't require us to define where we started and where we ended up. They just measure how far we traveled and how long it took to travel that far.

However, much of physics is about knowing where something is and how its position changes with time.

To define position we have to use a reference frame.

Position and Reference Frames

A reference frame lets us define where an object is located, relative to other objects.

For instance, we can use a map to compare the location of different cities, or a globe to compare the location of different continents.



However, not every reference frame is appropriate for every problem.

Reference Frame Activity

Send a volunteer out of the classroom to wait for further instructions.

Place an object somewhere in your classroom. Write specific directions for someone to be able to locate the object

Write them in a way that allows you to hand them to someone who can then follow them to the object.

Remember: you can't tell them the name of something your object is near, just how they have to move to get to it. For instance 'walk to the SmartBoard' is not a specific direction.

Test your directions out on your classmate, (who is hopefully still in the hallway!)

Reference Frame Activity - Reflection

In your groups, make a list of the things you needed to include in your directions in order to successfully locate the object in the room.

As a class, discuss your findings.



Results - Reference Frames

You probably found that you needed:

A starting poin(*tan origin*)

A set of direction(for instance left-right, forward-backward, up-down) A unit of measur(to dictate how far to go in each direction)

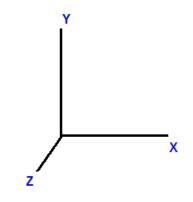
Results - Reference Frames

In this course, we'll usually:

Define the origin as a location labeled "zero"

Create three perpendicular axes : x, y and z for direction

Use the meter as our unit of measure



The Axis

In this course, we will be solving problems in one-dimension.

Typically, we use the x-axis for that direction.

+x will usually be to the right

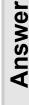
-x would then be to the left



We could define it the opposite way, but unless specified otherwise, this is what we'll assume. We also can think about compass directions in terms of positive and negative. For example, North would be positive and South negative.

The symbol for position is "x".

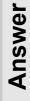
- 8 All of the following are examples of positive direction except:
 - \bigcirc A to the right
 - B north
 - \bigcirc C west
 - D up
 - ○E I need help





https://www.njctl.org/video/?v=JnzoLC8tbAE

- 9 All of the following are examples of negative direction except:
- \bigcirc A to the right
- ⊖ B south
- \bigcirc C west
- 🔾 D down
- \bigcirc E I need help





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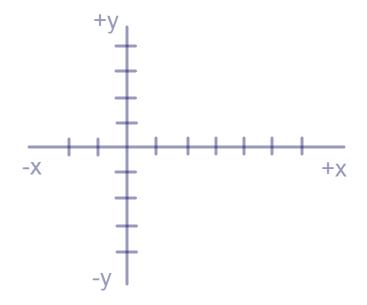
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Now that we understand how to define position, we can talk about a change in position; a displacement .

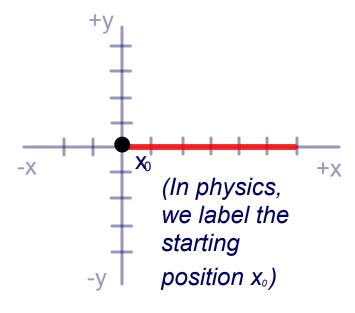
The symbol for "change" is the Greek letter "delta" " Δ ".

So " Δx " means the change in x or the change in position

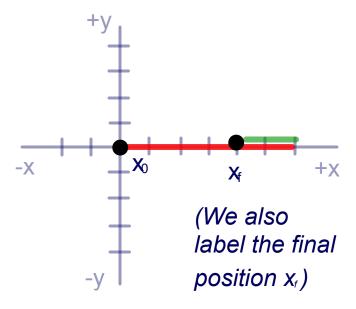
Displacement describes how far you are from where you started, regardless of how you got there.



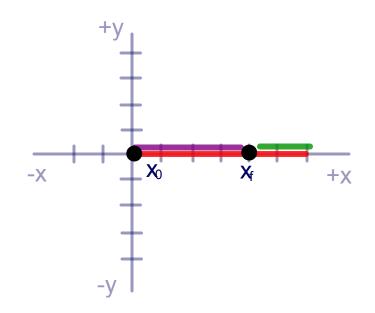
For instance, if you drive 60 miles from Pennsylvania to New Jersey...



and then 20 miles back toward Pennsylvania.



- You have traveled:
- a distance of 80 miles, and
- a displacement of 40 miles,
- since that is how far you are from where you started



we can calculate displacement with the following formula:

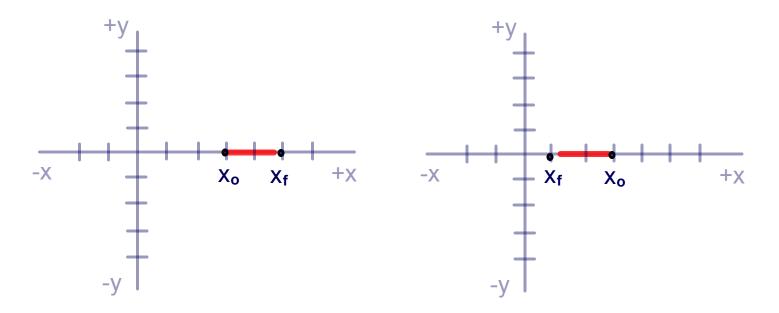
$$\Delta x = X_f - X_o$$

Measurements of distance can only be positive values (magnitudes) since it is impossible to travel a negative distance.



Imagine trying to measure a negative length with a meter stick...

However, displacement can be positive or negative since you can end up to the right or left of where you started.



Displacement is positive.

Displacement is negative.

Vectors and Scalars

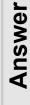
Scalar - a quantity that has only a magnitude (number or value)

Vector - a quantity that has both a magnitude and a direction

Which of the following are vectors? Scalars?

Quantity	Vector	Scalar
Time		
Distance		
Displacement		
Speed		

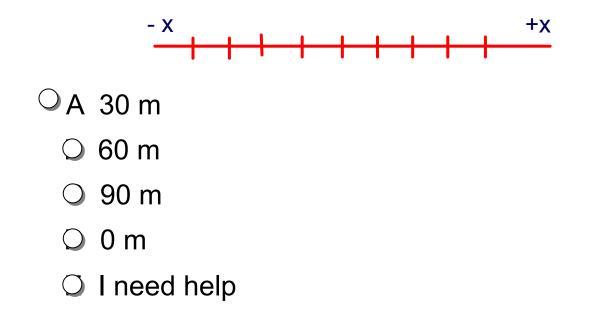
- 10 How far your ending point is from your starting point is known as:
 - A distance
 - B displacement
 - C a positive integer
 - D a negative integer
 - ○E I need help





https://www.njctl.org/video/?v=vxIWZ9_rQFo

11 A car travels 60m to the right and then 30m to the left. What distance has the car traveled?



Answer



https://www.njctl.org/video/?v=HxpHVhVbGF4

12 You travel 60m to the right and then 30m to the left. What is the magnitude (and direction) of your displacement?



- Q -30 m
- 0 m
- ○C 30 m
- ○D 60 m
- \bigcirc E I need help



Answer

- 13 Starting from the origin, a car travels 4km east and then 7 km west. What is the total distance traveled?
 - A 3 km
 - в -3 km
 - C 7 km
 - D 11 km
 - \bigcirc E I need help



- 14 Starting from the origin, a car travels 4km east and then 7 km west. What is the net displacement from the original point?
 - A 3 km west
 - B 3 km east
 - C 7 km west
 - D 11 km east
 - \bigcirc E I need help





- 15 You run around a 400m track. At the end of your run, what is the distance that you traveled?
 - \bigcirc A 0 m
 - ○B 100 m
 - ○C 200 m
 - ○D 400 m
 - ○E I need help





- 16 You run around a 400m track. At the end of your run, what is your displacement?
 - \bigcirc A 0 m
 - ○B 100 m
 - ○C 200 m
 - \bigcirc D 400 m
 - \bigcirc E I need help





Average Velocity





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https://njctl.org/video/?v=js6ZL6kBcsw

Average Velocity

Speed is defined as the ratio of distance and time

Average speed =	distance traveled	$s = \frac{d}{d}$
	time elapsed	t t

Similarly, velocity is defined as the ratio of displacement and time

	displacement	$-\Delta x$
Average velocity =	time elapsed	$v = \frac{1}{\Delta t}$

Average Velocity

Speeds are always positive, since speed is the ratio of distance and time; both of which are always positive.

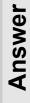
Average speed = $\frac{\text{distance traveled}}{\text{time elapsed}}$ $s = \frac{d}{t}$

But velocity can be *positive or negative*, since velocity is the ratio of displacement and time; and displacement can be negative or positive.

	displacement	Δx
Average velocity =	time elapsed	$v = \frac{1}{\Delta t}$

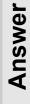
Usually, right is positive and left is negative.

- 17 Which of the following is a vector quantity?
 - \bigcirc A time
 - \bigcirc B velocity
 - C distance
 - D speed
 - \bigcirc E I need help





- 18 Average velocity is defined as change in _____ over a period of _____.
 - A distance, time
 - B distance, space
 - C position, time
 - D position, space
 - ○E I need help





https://www.njctl.org/video/?v=eIAG7H40utw

- 19 You travel 60 meters to the right in 20 s; what is your average velocity?
 - Q -3 m/s
 - +0.3 m/s
 - +3 m/s
 - +6 m/s
 - I need help



https://www.njctl.org/video/?v=IMTx61aMxPo

- 20 An elephant travels 60 meters to the left in 20 s; what is the average velocity?
 - ○A -3 m/s
 - \bigcirc B 0 m/s
 - ○C +3 m/s
 - ○D +6 m/s
 - ○E I need help



https://www.njctl.org/video/?v=0UbmRkIJWwU

21 You travel 60 meters to the left in 20 s and then you travel 60 meters to the right in 30 s; what is your average velocity?

Answer

 \odot A -3 m/s

○B -2 m/s

○C 0 m/s

○D +3 m/s

○E I need help



https://www.njctl.org/video/?v=NQ0nOZFCKZI

- 22 You travel 60 meters to the left in 20 s and then you travel 60 meters to the right in 30 s; what is your average speed?
 - Q 0 m/s
 - 1.8 m/s
 - 2.4 m/s
 - 3.2 m/s

◯ I need help



https://www.njctl.org/video/?v=i_iJgYVaRh8

23 You run completely around a 400 m track in 80s. What was your average speed?

○A 0 m/s

○B 4 m/s

 \bigcirc C 5 m/s

○D 8 m/s

\bigcirc E I need help

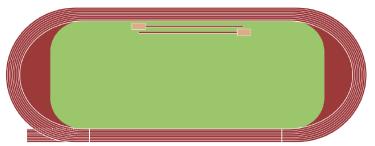


https://www.njctl.org/video/?v=doZMr5s0mgo

- 24 You run completely around a 400 m track in 80s. What was your average velocity?
 - Q 0 m/s
 - ⊖ +4 m/s
 - +5 m/s
 - +8 m/s

○ I need help





25 You travel 160 meters in 60 s; what is your average speed?

 \bigcirc A 0 m/s

○B 2.7 m/s

[◯]C 6.3 m/s

○D 16.7 m/s

○E I need help





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Sometimes the average velocity is all we need to know about an object's motion.

For example:

A race along a straight line is really a competition to see whose average velocity is the greatest.

The prize goes to the competitor who can cover the displacement in the shortest time interval.



But the average velocity of a moving object can't tell us how fast the object moves at any given point during the interval Δt .

Average velocity is defined as change in position over time. This tells us the 'average' velocity for a given length or *span* of time.



If we want to know the speed or velocity of an object at a *specific point in time* (with this radar gun for example), we want to know the instantaneous velocity...

Watch what happens when we look for the instantaneous velocity by reducing the amount of time we take to measure displacement.

Displacement	Time	Velocity
100m	10 s	

In an experiment, an object travels at a constant velocity. Find the magnitude of the velocity using the data above.

Displacement	Time	Velocity
100m	10 s	10 m/s
10 m	1 s	

What happens if we measure the distance traveled in the same experiment for only one second?

What is the velocity?

Displacement	Time	Velocity
100m	10 s	10 m/s
10 m	1 s	10 m/s
0.001m	0.0001 s	

What happens if we measure the distance traveled in the same experiment for a really small time interval?

What is the velocity?

Displacement	Time	Velocity
100 m	10 s	10 m/s
10 m	1 s	10 m/s
1.0 m	0.10 s	10 m/s
0.10 m	0.010 s	10 m/s
0.010 m	0.0010 s	10 m/s
0.0010 m	0.00010 s	10 m/s
0.00010 m	0.000010 s	10 m/s

Since we need time to measure velocity, we can't know the exact velocity "at" a particular time... but if we imagine a really small value of time and the distance traveled, we can estimate the instantaneous velocity.

To describe the motion in greater detail, we need to define the velocity at any specific instant of time or specific point along the path. Such a velocity is called instantaneous velocity.

Note that the word *instant* has somewhat different meaning in physics than in everyday language. Instant is not necessarily something that is finished quickly. We may use the phrase "It lasted just an instant" to refer to something that lasted for a very short time interval.







In physics an instant has no duration at all; it refers to a single value of time.

One of the most common examples we can use to understand instantaneous velocity is driving a car and taking a quick look on the speedometer.

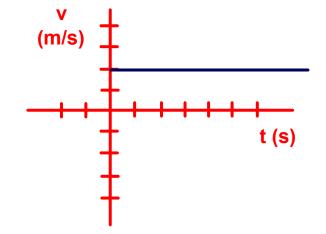
At this point, we see the instantaneous value of the velocity.



The instantaneous velocity is the same as the magnitude of the average velocity as the time interval becomes very very short.

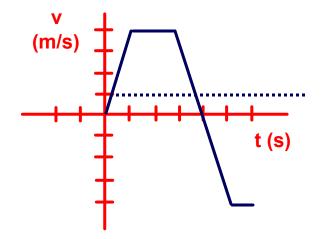
$$v = \frac{\Delta x}{\Delta t}$$
 as $\Delta t = 0$

The graph below shows velocity versus time.

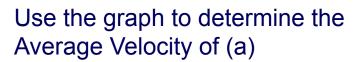


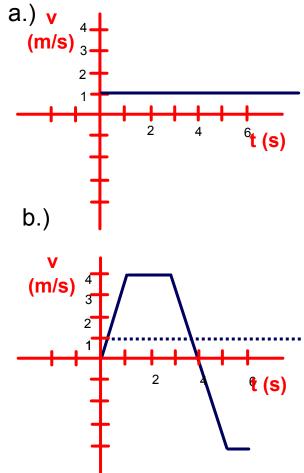
How do you know the velocity is constant?

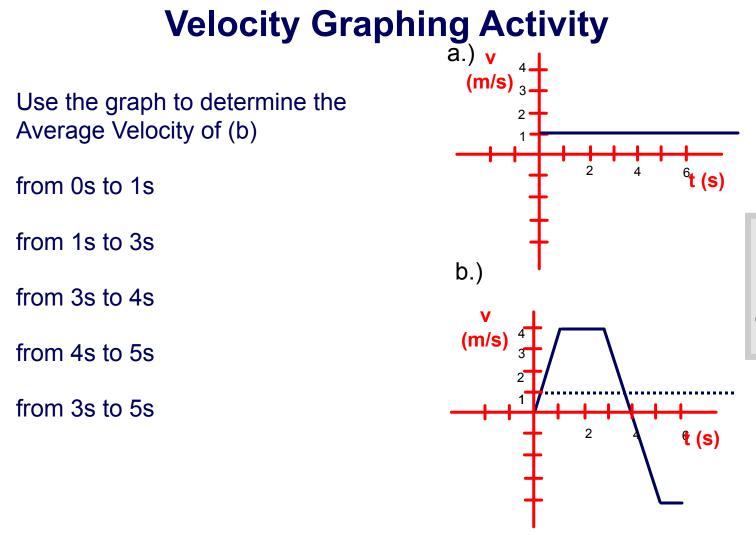
The graph below shows velocity versus time.



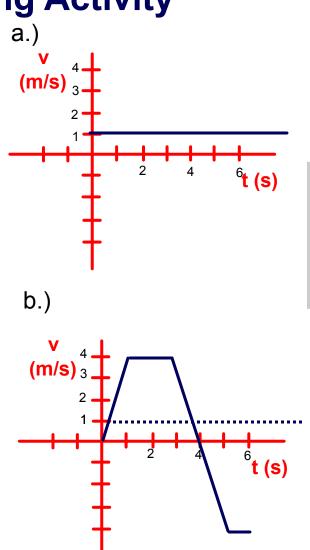
When is the velocity increasing? Decreasing? Constant? Discuss.



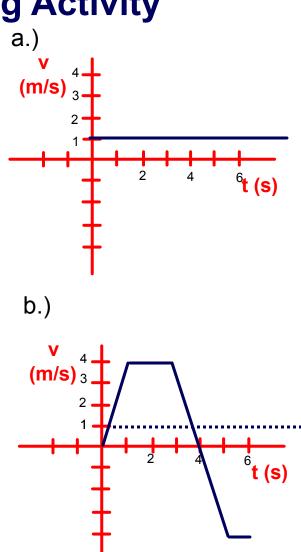




Use the graph to determine the Instantaneous Velocity of (a) at 2 seconds



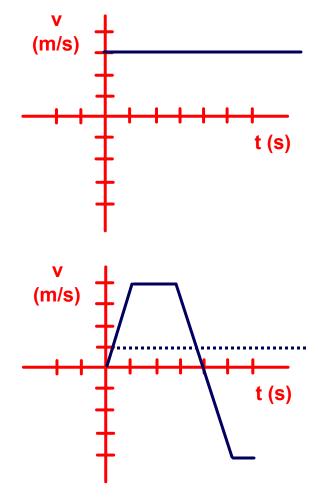
Use the graph to determine the Instantaneous Velocity of (b) at 2 seconds



These graphs show (a) constant velocity and (b) varying velocity.

(a) When the velocity of a moving object is a constant the instantaneous velocity is the same as the average.

(b) When the velocity of a moving object changes its instantaneous velocity is different from the average velocity.



Acceleration



https://www.njctl.org/video/?v=jGbVA3e9Op4

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Acceleration

Acceleration is the rate of change of velocity.



Acceleration

 $a = \frac{v - v_o}{t}$

Acceleration is a vector, although in one-dimensional motion we only need the sign.

Since only constant acceleration will be considered in this course, there is no need to differentiate between average and instantaneous acceleration.

Units for Acceleration

Units for acceleration

You can derive the units by substituting the correct units into the right hand side of these equations.

$$a = \frac{\Delta v}{\Delta t}$$
 $---- \frac{m/s}{s} = m/s^2$

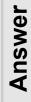
- 26 Acceleration is the rate of change of _____
- A displacement
- B distance
- \bigcirc C speed
- D velocity
- \bigcirc E I need help





https://www.njctl.org/video/?v=4tmNAmswOd0

- 27 The unit for velocity is:
 - \bigcirc A m
 - ⊖ B m/s
 - ◯ C m/sੰ
 - ◯ D ft/sੰ
 - \bigcirc E I need help

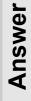




https://www.njctl.org/video/?v=D-h5qV2Plys

28 The metric unit for acceleration is:

- ⊖A m
- ⊖B m/s
- OC m/s
- ◯D ft/s
- \bigcirc E I need help





https://www.njctl.org/video/?v=EMkc2W5u6vw

- A horse gallops with a constant acceleration of 3m/s². Which statement below is true?
 - \bigcirc A The horse's velocity doesn't change.
 - \bigcirc B The horse moves 3m every second.
 - C The horse's velocity increases 3m every second.
 - \bigcirc D The horse's velocity increases 3m/s every second.
 - \bigcirc E I need help



https://www.njctl.org/video/?v=CbtjHuAk-Ew

Solving Problems

After you read the problem carefully:

- 1. Draw a diagram (include coordinate axes).
- 2. List the given information.
- 3. Identify the unknown (what is the question asking?)
- 4. Choose a formula (or formulas to combine)
- 5. Rearrange the equations to isolate the unknown variable.
- 6. Substitute the values and solve!

7. Check your work. (You can do the same operations to the units to check your work ... try it!)



- 30 Your velocity changes from 60 m/s to the right to 100 m/s to the right in 20 s; what is your average acceleration?
 - ⊖A -2 m/s²
 - ○B 0 m/s²
 - ⊖C +2 m/s²
 - ○D +4 m/s²
 - ○E I need help



- 31 Your velocity changes from 60 m/s to the right to 20 m/s to the right in 20 s; what is your average acceleration?
 - ⊖A -2 m/s²
 - ○B 0 m/s²
 - ^OC +2 m/s²
 - ○D +4 m/s²
 - ○E I need help



https://www.njctl.org/video/?v=Dm5nPrPW_v4

32 Your velocity changes from 50 m/s to the left to 10 m/s to the right in 15 s; what is your average acceleration?

⊖A -3 m/s²

- ○B 0 m/s²
- ^OC +4 m/s²
- ○D +5 m/s²
- ○E I need help



33 Your velocity changes from 90 m/s to the right to 20 m/s to the right in 5.0 s; what is your average acceleration?

⊖A -14 m/s²

○B -7 m/s²

 \bigcirc C 0 m/s²

○D +14 m/s²

○E I need help

Kinematics Equation 1



https://www.njctl.org/video/?v=69S2wEpXyAU

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Motion at Constant Acceleration

$a = \frac{\Delta v}{\Delta t}$	but since " Δ " means change
	$\Delta v = v - v_{\circ}$ and
V - V _o	$\Delta t = t - t_{\circ}$
$a = \frac{v - v_o}{t}$	if we always let $t_{\circ} = 0$, $\Delta t = t$
at = v - y	
v-v o = at	Solving for "v"
$v = v_o + at$	

This equation tells us how an object's velocity changes as a function of time.

- 34 Starting from rest, you accelerate at 4.0 m/s² for6.0s. What is your final velocity?
 - ⊖A +4 m/s
 - ○B +16 m/s
 - ○C +24 m/s
 - ○D +32 m/s
 - ○E I need help



https://www.njctl.org/video/?v=my2wda8jQn0

- 35 Starting from rest, you accelerate at 8.0 m/s² for9.0s. What is your final velocity?
 - Q +8 m/s
 - +9 m/s
 - +72 m/s
 - +81 m/s

○ I need help



- 36 You have an initial velocity of 5.0 m/s. You then experience an acceleration of -1.5 m/s² for 4.0s; what is your final velocity?
 - Q -6 m/s
 - ◯ -1 m/s
 - +1 m/s
 - +11 m/s
 - I need help



https://www.njctl.org/video/?v=X_jWqMS3myk

- 37 You have an initial velocity of -3.0 m/s. You then experience an acceleration of 2.5 m/s² for 9.0s; what is your final velocity?
 - Q -3.5 m/s
 - +18.4 m/s
 - +19.5 m/s
 - +27.9 m/s



I need help

https://www.njctl.org/video/?v=DREeRklptKl

38 How much time does it take to accelerate from an initial velocity of 20m/s to a final velocity of 100m/s if your acceleration is 1.5 m/s²?

Q 20.7 s

◯ 32.4 s

○ 53.3 s

○ 80.1 s

○ I need help



https://www.njctl.org/video/?v=J4FZ8vf_RSw

- 39 How much time does it take to come to rest if your initial velocity is 5.0 m/s and your acceleration is -2.0 m/s²?
 - Q 1.5 s
 - ◯ 2 s
 - 2.5 s

○ 5 s

○ I need help



https://www.njctl.org/video/?v=1EQ_eMYq9pQ

- 40 An object accelerates at a rate of 3 m/s² for 6 s until it reaches a velocity of 20 m/s. What was its initial velocity?
 - ○A 0 m/s
 - ○B 2 m/s
 - ○C 8 m/s
 - ○D 18 m/s



E I need help

- 41 An object accelerates at a rate of 1.5 m/s² for 4 s until it reaches a velocity of 10 m/s. What was its initial velocity?
 - Q 0 m/s
 - ◯ 2 m/s
 - 4 m/s
 - 6 m/s

○ I need help



https://www.njctl.org/video/?v=-q-YF4pzxBM

Graphing Motion at Constant Acceleration

In physics there is another approach in addition to algebraic which is called graphical analysis. The formula $v = v_0 + at$ can be interpreted by the graph. We just need to recall our memory from math classes where we already saw a similar formula y = mx + b.

From these two formulas we can make some analogies:

- $v \Rightarrow y$ (dependent variable of x),
- $v_{\circ} \Rightarrow b$ (intersection with vertical axis),
- $t \Rightarrow x$ (independent variable),
- $a \Rightarrow m$ (slope of the graph- the ratio between rise and run $\Delta y/\Delta x$).

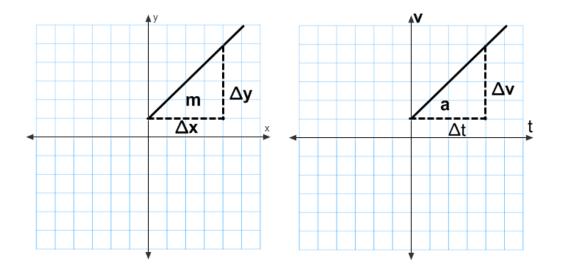


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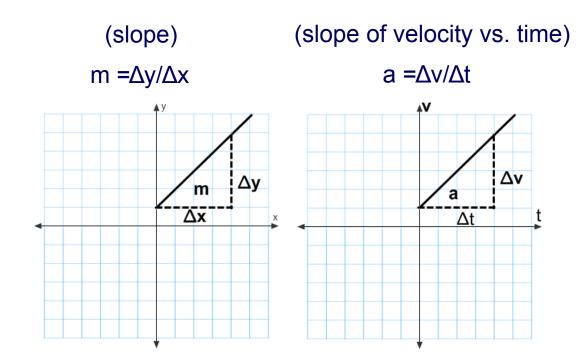
Below we can find the geometric explanation to the acceleration $a = \Delta v / \Delta t$.

If slope is equal to: $m = \Delta y / \Delta x$

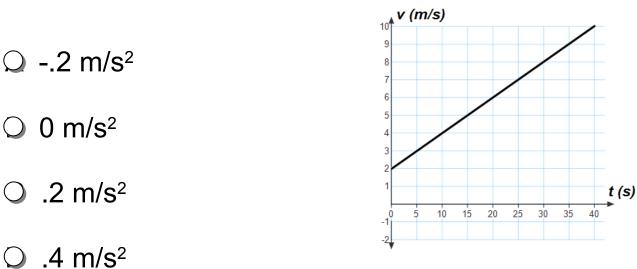
Then consider a graph with velocity on the y-axis and time on the x-axis. What is the slope for the graph on the right?



The graph on the right has a slope $\Delta v/\Delta t$, which is equal to acceleration. Therefore, the slope of a velocity vs. time graph is equal to acceleration.



42 The velocity as a function of time is presented by the graph. What is the acceleration?



Answer

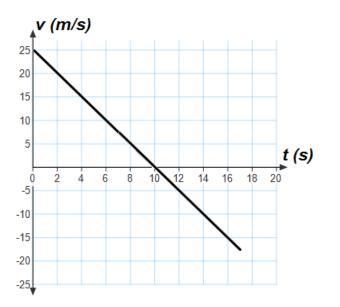
◯ I need help



- 43 The velocity as a function of time is presented by the graph. Find the acceleration.
 - 2.5 m/s²
 0 m/s²
 2.5 m/s²
 5 m/s²

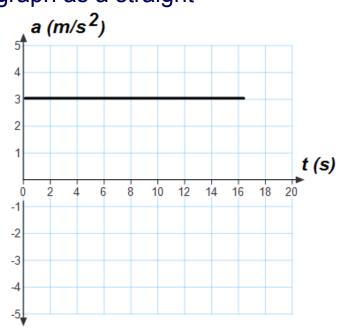
○ 5 m/s² ○ I need help

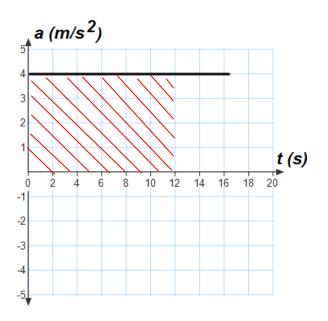




The acceleration graph as a function of time can be used to find the velocity of a moving object. When the acceleration is constant the velocity is changing by the same amount each second. This can be shown on the graph as a straight horizontal line. $a (m/s^2)$

In order to find the change in velocity for a certain limit of time we need to calculate the area under the acceleration line that is limited by the time interval.



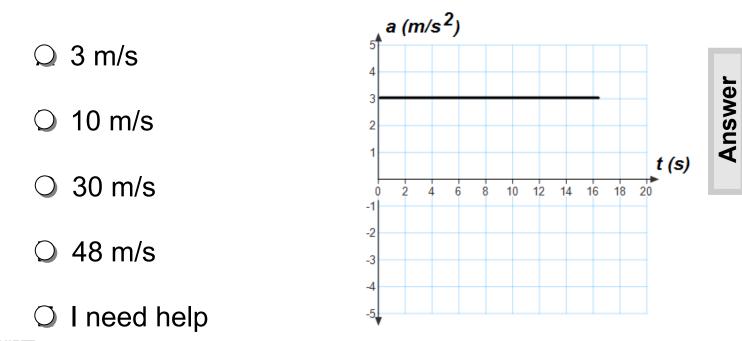


The change in velocity during first 12 seconds is equivalent to the shadowed area

$$(4m \times 12s = 48m).$$

The change in velocity during first 12 seconds is 48 m/s.

44 The following graph shows acceleration as a function of time of a moving object. What is the change in velocity during first 10 seconds?





https://www.njctl.org/video/?v=D3bQyx0ygFM

Free Fall: Acceleration Due to Gravity





https://www.njctl.org/video/?v=rB95M_Rgmq8

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Free Fall

y 🖡

All unsupported objects fall towards Earth with the same acceleration. We call this acceleration the "acceleration due to gravity" and it is denoted by g.

 $g = 9.8 \text{ m/s}^2$

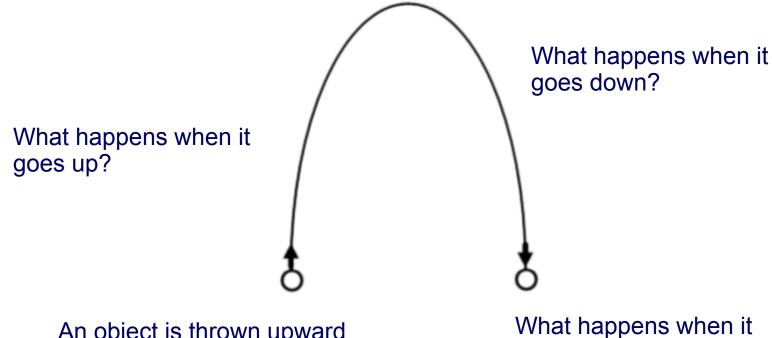
Keep in mind, ALL objects accelerate towards the earth at the same rate.



Click here to watch Galileo's famous experiment performed on the moon free fall demo sheet

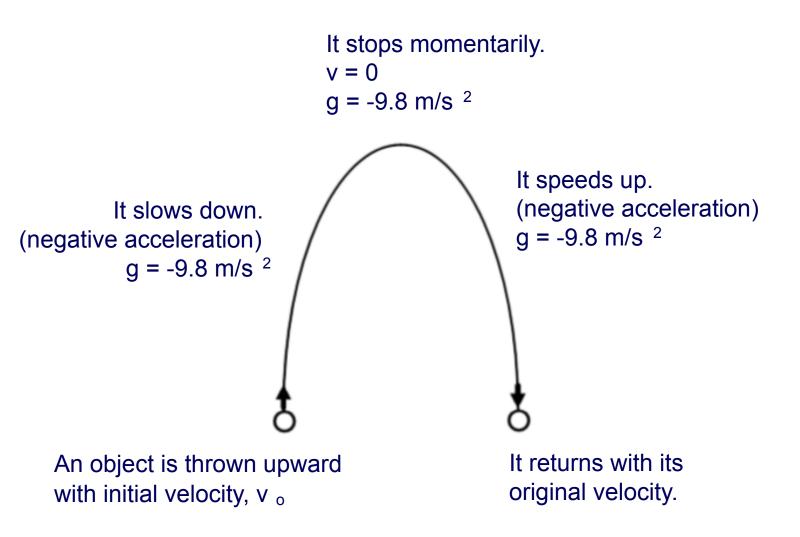
Free Fall

What happens at thep?



An object is thrown upward with initial velocity, v. (Click on question for answer.) What happens when it lands?

Free Fall Answers

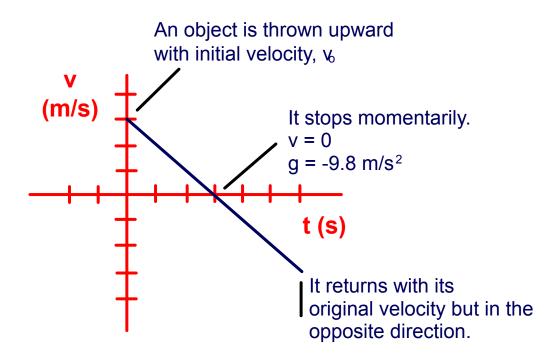


Free Fall

On the way up:			On the way down: $v_1 a t = 0 s$		
V	a	t = 3 s	V ₁	a	t = 0 s
V ₂	a	t = 2 s	I	V 1	t=1s
V ₁	a	t = 1 s	V ₂	а	t = 1 s
			v	V ₂	t = 2 s
V ₀	V ₁	t = 0 s			
I	I	t = 0 s		V	t = 3 s

Free Fall

For any object thrown straight up into the air, this is what the velocity vs. time graph looks like.



- 45 A ball is dropped from rest and falls (do not consider air resistance). Which is true about its motion?
 - A acceleration is constant
 - B acceleration is decreasing
 - C speed is constant
 - \bigcirc D speed is descreasing
 - ○E I need help





https://www.njctl.org/video/?v=lqrx6l6fFPo

- 46 An acorn falls from an oak tree. You note that it takes 2.5 seconds to hit the ground. How fast was it going when it hit the ground?
 - ◯A 2.5 m/s
 - ○B 4.8 m/s
 - ⊖C 9.8 m/s
 - ○D 25 m/s
 - \bigcirc E I need help





- 47 A rock falls off a cliff and hits the ground 5 seconds later. What velocity did it hit the ground with?
 - ○A -23 m/s
 - ○B -49 m/s
 - ^OC -98 m/s
 - ○D -496 m/s
 - \bigcirc E I need help





https://www.njctl.org/video/?v=qSo50sEyALQ

- 48 A ball is thrown down off a bridge with a velocity of 5 m/s. What is its velocity 2 seconds later?
 - Q -4.8 m/s
 - -14.8 m/s
 - -19.6 m/s
 - -24.6 m/s
 - I need help





https://www.njctl.org/video/?v=_ush_fkVoyk

49 An arrow is fired into the air and it reaches its highest point 3.0 seconds later. What was its velocity when it was fired?

◯A +9.8 m/s

- ○B +29.4 m/s
- ○C +58.4 m/s
- ○D +98 m/s
- ○E I need help



https://www.njctl.org/video/?v=6CXXQIqCZro

- 50 A rocket is fired straight up from the ground. It returns to the ground 10 seconds later. What was its launch speed?
 - Q 9.8 m/s
 - 49 m/s
 - 98 m/s
 - ◯ 147 m/s
 - I need help



If velocity is changing at a constant rate, the average velocity is just the average of the initial and final velocities.

And we learned earlier that

Some problems can be solved most easily by using these two equations together.

 $\overline{v} = \frac{v + v_o}{2}$

$$\overline{v} = \frac{\Delta x}{t}$$

$$\frac{\Delta x}{t} = \frac{v + v_0}{2}$$

$$\Delta x = \frac{(v + v_0)}{2} t$$



- 51 Starting from rest you accelerate to 20 m/s in 4.0s. What is your average velocity?
 - Q +4 m/s
 - +10 m/s
 - +15 m/s
 - +20 m/s
 - I need help



https://www.njctl.org/video/?v=RbtF1rQASGw

- 52 Starting with a velocity of 12 m/s you accelerate to 48 m/s in 6.0s. What is your average velocity?
 - Q +12 m/s
 - +24 m/s
 - +30 m/s
 - +48 m/s
 - I need help



https://www.njctl.org/video/?v=DnHDGc5cAh0

53 Starting with a velocity of 12 m/s you accelerate to 48 m/s in 6.0s. Using your previous answer, how far did you travel in that 6.0s?

> Previous Answer average velocity = 30 m/s

○ 81 m

○ 72 m

- 120 m
- 🔾 180 m



○ I need help

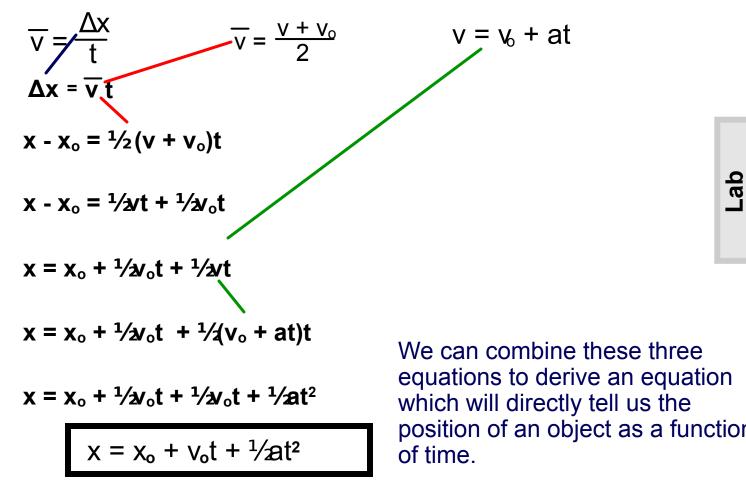
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Kinematics Equation 2

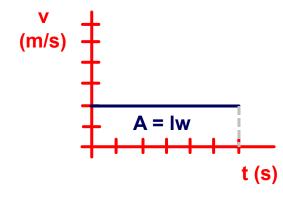


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Graphical Approach

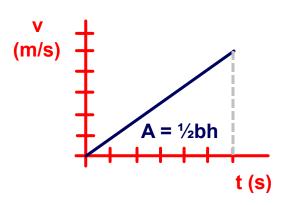


If the area under the graph is length x width (A = Iw), then:

A = $v_0 t$ Since we know that $v = \frac{\Delta x}{t}$, then area is really Δx .

 $A = \Delta x = v_0 t$

Motion at Constant Acceleration Graphical Approach

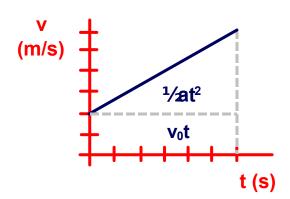


If the area under this graph is $\frac{1}{2}$ base x height, then:

A = $\frac{1}{2}t\Delta v$ Since we know that a = $\frac{\Delta v}{t}$, Δv = at.

 $A = \Delta x = \frac{1}{2}t(at) = \frac{1}{2}at$

Graphical Approach



Therefore, the area under a velocity vs. time graph is displacement. It can be calculated by combining the previous two results.

$$A = \Delta x = v_0 t + \frac{1}{2} a t^2$$

 $x - x_0 = v_0 t + \frac{1}{2} a t^2$

 $x = x_0 + v_0 t + \frac{1}{2} a t^2$

- 54 An airplane starts from rest and accelerates at a constant rate of 3.0 m/s² for 30.0 s before leaving the ground. How far did it move along the runway?
 - ○A 90 m
 - ○B 270 m
 - ○C 1350 m
 - ○D 2700 m







55 A Volkswagen Beetle moves at an initial velocity of 12 m/s. It coasts up a hill with a constant acceleration of –1.6 m/s². How far has it traveled after 6.0 seconds?

⊖A 2.4 m

○B 28.8 m

○C 43.2 m

○D 60 m







https://www.njctl.org/video/?v=lv8l_-RG_fY

- 56 A motorcycle starts out from a stop sign and accelerates at a constant rate of 20 m/s². How long will it take the motorcycle to go 300 meters?
 - OA 5s
 - ○B 5.5 s
 - ^OC 17.3 s
 - ○D 30 s
 - ○E I need help





- 57 A train pulling out of Grand Central Station accelerates from rest at a constant rate. It covers 800 meters in 20 seconds. What is its rate of acceleration?
 - \bigcirc 4 m/s²
 - \bigcirc 5 m/s²
 - \bigcirc 10 m/s²
 - \bigcirc 20 m/s²





58 A car has an initial velocity of 45 m/s. It accelerates for 4.8 seconds. In this time, the car covers 264 meters. What is its rate of acceleration?

Q 0.52 m/s²

○ 1.0 m/s²

○ 2.1 m/s²

○ 4.2 m/s²



I need help

https://www.njctl.org/video/?v=Kcw5NEHp2zg

- 59 A Greyhound bus traveling at a constant velocity starts to accelerate at a constant 2.0 m/s². If the bus travels 500 meters in 20 seconds, what was its initial velocity?
 - Q 2 m/s
 - 2.5 m/s
 - 5 m/s
 - 24 m/s

○ I need help



https://www.njctl.org/video/?v=MQxR6xG-AiM

Kinematics Equation 3



https://www.njctl.org/video/?v=Uk8LcZ1WIxg

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Motion at Constant Acceleration

We can also combine these equations so as to eliminate:

$$v^2 = v_o^2 + 2a(x - x_o)$$

60 A car accelerates from rest to 30m/s while traveling a distance of 20m; what was its acceleration?

Q 22.5 m/s²

○ 30 m/s²

○ 45 m/s²

○ 90 m/s²

○ I need help



s://www.njctl.org/video/?v=RNQxw3-mQCU

- 61 You accelerate, from rest, at 10m/s for a distance of 100m; what is your final velocity?
 - Q 20.3 m/s
 - ◯ 44.7 m/s
 - 84.3 m/s
 - ◯ 100 m/s
 - I need help



https://www.njctl.org/video/?v=kZBFio3GHFY

62 You accelerate from 20m/s to 60m/s while traveling a distance of 200m; what was your acceleration?

Q 2 m/s²

- 4 m/s²
- 8 m/s²
- 20 m/s²

○ I need help



https://www.njctl.org/video/?v=z2Y9RQqk_I0

63 Beginning with a velocity of 25m/s, you accelerate at a rate of 2.0m/s². During that acceleration you travel 200m; what is your final velocity?

Q 2.1 m/s

- 25.3 m/s
- 37.7 m/s
- 50.4 m/s
- I need help



- 64 A dropped ball falls -8.0m; what is its final speed?
 - Q 8.2 m/s
 - ◯ 10.3 m/s
 - 12.5 m/s
 - 17.2 m/s
 - ◯ I need help



https://www.njctl.org/video/?v=v7dJTLjftrE

65 A ball with an initial velocity of 25m/s is subject to an acceleration of -9.8 m/s²; how high does it go before coming to a momentary stop?

○A 25.4 m

○B 31.9 m

[⊖]C 62.5 m

○D 248.8 m

○E I need help



https://www.njctl.org/video/?v=ReTH6IKoUYs

Motion at Constant Acceleration

We now have all the equations we need to solve constant-acceleration problems.

$$v = v_o + at$$

$$x = x_0 + v_0 t + \frac{1}{2}at^2$$

$$v^2 = v_0^2 + 2a(x - x_0)$$



https://www.njctl.org/video/?v=S4VkyTF8uBg

Mixed Kinematics Problems

Return to Table of Contents 66 An arrow is projected by a bow vertically up with a velocity of 40 m/s, and reaches a target in 3 s. How high is the target located?

Q 12.7 m

🔾 60.6 m

○ 75.9 m

○ 120.2 m

○ I need help



https://www.njctl.org/video/?v=OVCqcjGQEwY

67 An object accelerates from rest, with a constant acceleration of 8.4 m/s², what will its velocity be after 11s?

○A 81.1 m/s

○B 84.9 m/s

[◯]C 92.4 m/s

○D 198.3 m/s

○E I need help



https://www.njctl.org/video/?v=D7wd9ctbXkM

68 An object accelerates from rest to a velocity of 34 m/s over a distance of 70 m. What was its acceleration?

Q 8.3 m/s²

○ 10 m/s²

○ 17 m/s²

○ 36 m/s²

○ I need help







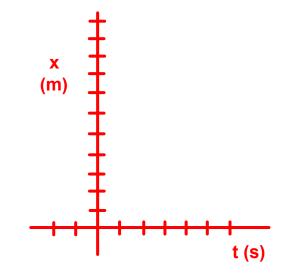
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Position vs Time Graphs

An object's position at any point in time can be graphed.

These graphs show position but also can be used to find an object's velocity.

Position is the dependent variable (y-axis), and time is the independent variable (x-axis).



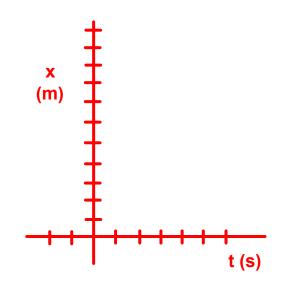
Creating a Position vs. Time Graph

1. Draw a cartesian coordinate system by drawing a vertical and horizontal axis.

2. Label the vertical axis as position (x), and the horizontal axis as time (t).

3. Add units next to each axis label, showing position measured in meters, and time measured in seconds

4. Add points to the graph requires both the position and time it happened.

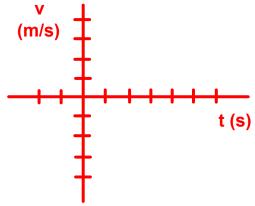


Velocity vs. Time Graphs

Similarly, the same approach can be used to create a velocity vs. time graph.

A velocity versus time graph differs by having the velocity on the vertical axis.

A velocity versus time graph shows describes an objects velocity, it's displacement, and acceleration.



Starting at the position, $x_0 = 4$ m, you travel at a constant velocity of +2 m/s for 6s.

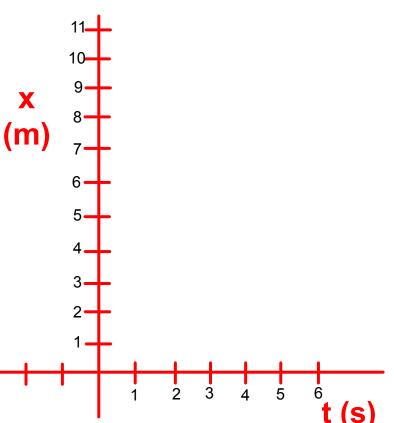
a. Determine your position at the times of 0s; 2s; 5s; and 6s.

Starting at the position, $x_0 = 4$ m, you travel at a constant velocity of +1 m/s for 6s.

b. Draw the Position versus Time for your travel during this time.

Drag and drop the data points on the graph in order to construct the v vs t pattern!

Draw a line of best fit to observe the pattern.



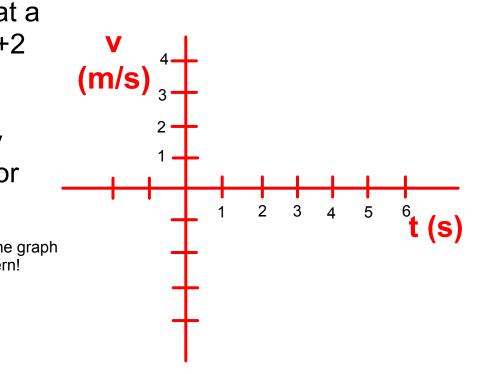
Starting at the position, $x_0 = 4$ m, you travel at a constant velocity of +2 m/s for 6s.

c. Draw the Velocity versus Time graph for your trip.

Drag and drop the data points on the graph in order to construct the v vs t pattern!

• • • • • •

Draw a line of best fit to observe the pattern.

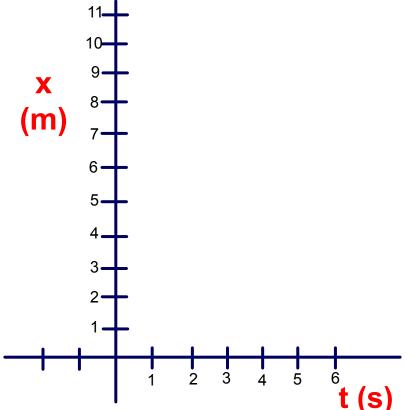


Starting at the position, $x_0 = 10$ m, you travel at a constant velocity of -1m/s for 6s.

d. Draw the Position versus Time for your travel during this time.

Drag and drop the data points on the graph in order to construct the v vs t pattern!

Draw a line of best fit to observe the pattern.

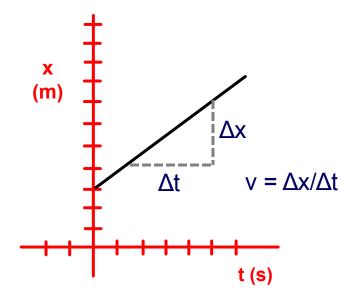


Analyzing Position vs Time Graphs

Recall earlier in this unit that slope was used to describe motion.

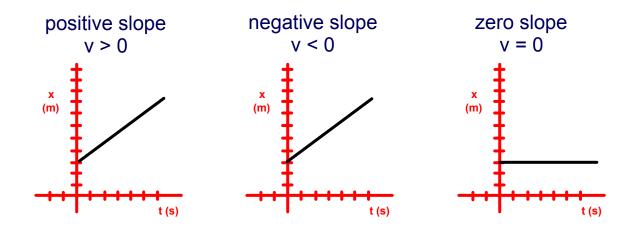
The slope in a position vs. time graph is $\Delta x/\Delta t$, which is equal to velocity.

Therefore, slope is equal to velocity on a position vs. time graph.



Analyzing Position vs Time Graphs

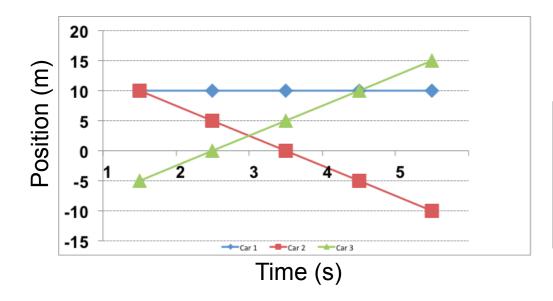
A positive slope is a positive velocity, a negative slope is a negative velocity, and a slope of zero means zero velocity.



A positive velocity means moving in the positive direction, a negative velocity means moving in the negative direction, and zero velocity means not moving at all.

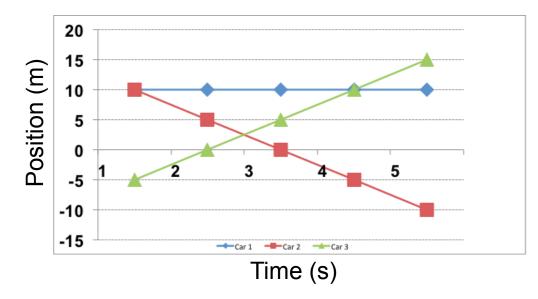
The position versus time graph, below, describes the notion of three different cars moving along the x-axis.

a. Describe, in words, the velocity of each of the cars. Make sure you discuss each car's speed and direction.



The position versus time graph, below, describes the otion of three different cars moving along the x-axis.

b. Calculate the velocity of each of the cars.

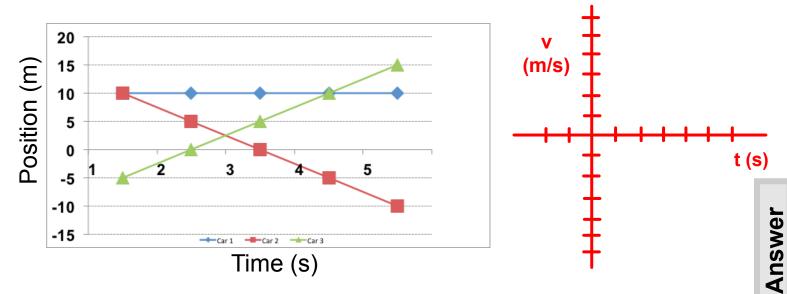


Answer

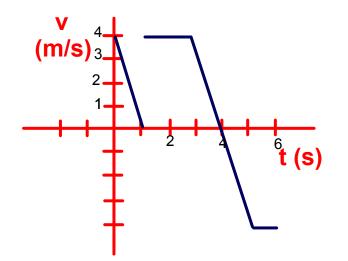


https://www.njctl.org/video/?v=0z2PvzGoFGo

c. Draw, on one set of axes, the Velocity versus Time graph for each of the three cars.



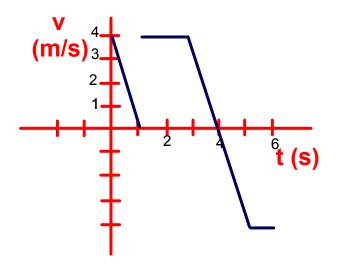
69 When is velocity zero?



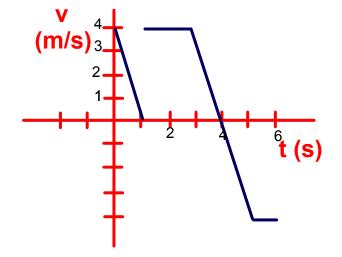




https://www.njctl.org/video/?v=W3YyvDwwBbc



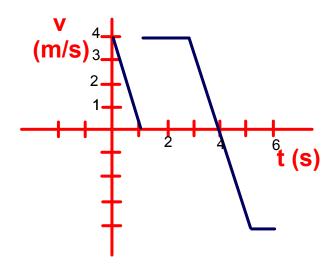
Describe in words what is happening to the speed during the following intervals. a) 0s to 1s b) 1s to 3s c) 3s to 4 sec d) 4s to 5s e) 5s to 6s



Determine the average speed during the following intervals. a) 0s to 1s b) 1s to 3s c) 3s to 4 sec d) 4s to 5s e) 5s to 6s f) 3s to 5s



https://www.njctl.org/video/?v=Lqhl24yBB0E



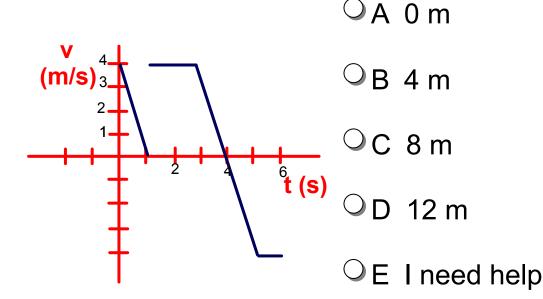
a) 0s to 1s
$$V_{avg} = +2m/s$$

b) 1s to 3s $V_{avg} = +4m/s$
c) 3s to 4s $V_{avg} = +2m/s$
d) 4s to 5s $V_{avg} = -2m/s$
e) 5s to 6s $V_{avg} = -4m/s$
f) 3s to 5s $V_{avg} = 0m/s$

 $V_{1} = (V_{1} + V_{2})/2$

Determine the displacement during the following intervals. a) 0s to 1s b) 1s to 3s c) 3s to 4 sec d) 4s to 5s e) 5s to 6s





71 Determine the net displacement during the first four seconds of travel.

Answer



https://www.njctl.org/video/?v=eZAznYcQQ7s

Summary

• Kinematics is the description of how objects move with respect to a defined reference frame.

· Displacement is the change in position of an object.

• Average speed is the distance traveled divided by the time it took; average velocity is the displacement divided by the time.



https://www.njctl.org/video/?v=iyQH4q1hbUU

Summary (continued)

- Instantaneous velocity is the limit as the time becomes infinitesimally short.
- Average acceleration is the change in velocity divided by the time.
- Instantaneous acceleration is the limit as the time interval becomes infinitesimally small.

Summary (continued)

 There are four equations of motion for constant acceleration, eacl requires a different set of quantities.

$$v = v_o + at$$

$$x = x_0 + v_0 t + \frac{1}{2} a t^2$$

$$v^2 = v_0^2 + 2a(x - x_0)$$

$$\overline{v} = \frac{v + v_o}{2}$$